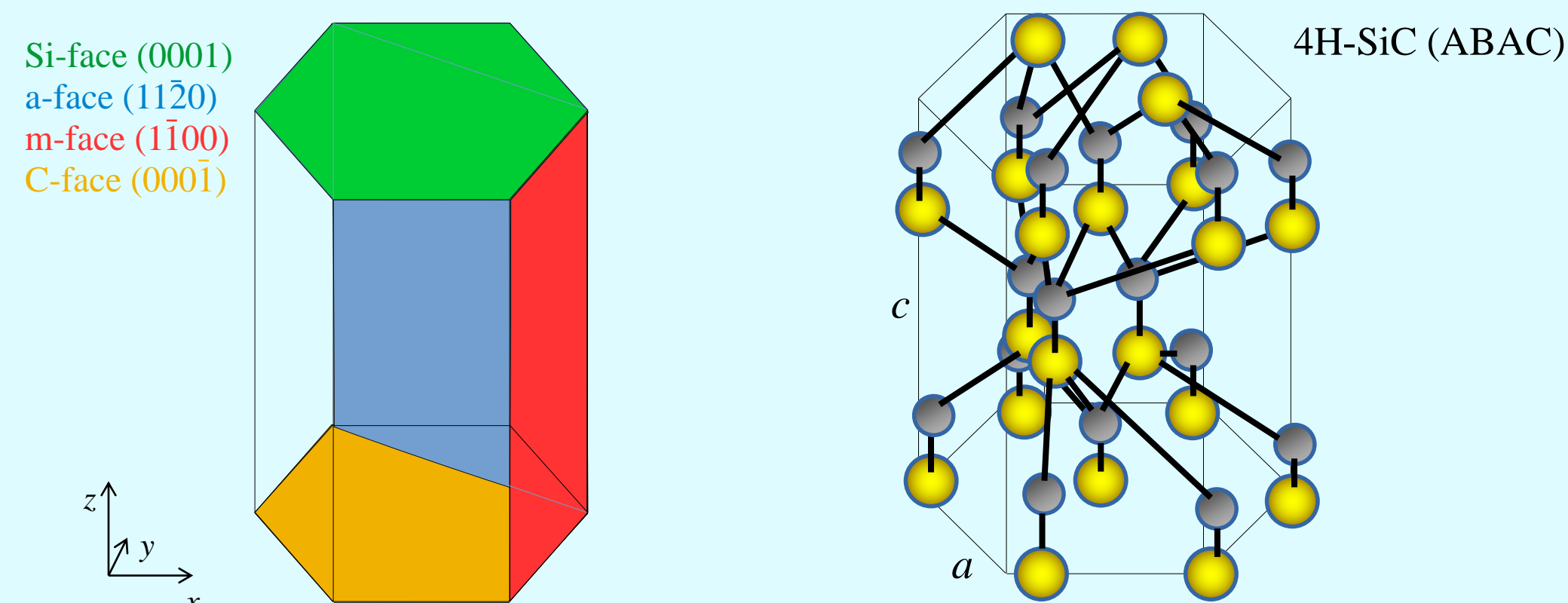


Introduction

- We propose a direction dependent interpolation method for silicon carbide (SiC) oxidation growth rates.
- The rates for the three-dimensional simulations are computed according to the four known growth rate values.
- Our approach is an essential step towards highly accurate three-dimensional oxide growth simulations and helps to better understand the silicon carbide anisotropic nature and oxidation mechanism.



Thermal Oxidation Models

Deal-Grove [1]

$$\frac{dX}{dt} = \frac{B}{A+2X}$$

Massoud empirical relation [2]

$$\frac{dX}{dt} = \frac{B}{A+2X} + C \exp\left(-\frac{X}{L}\right)$$

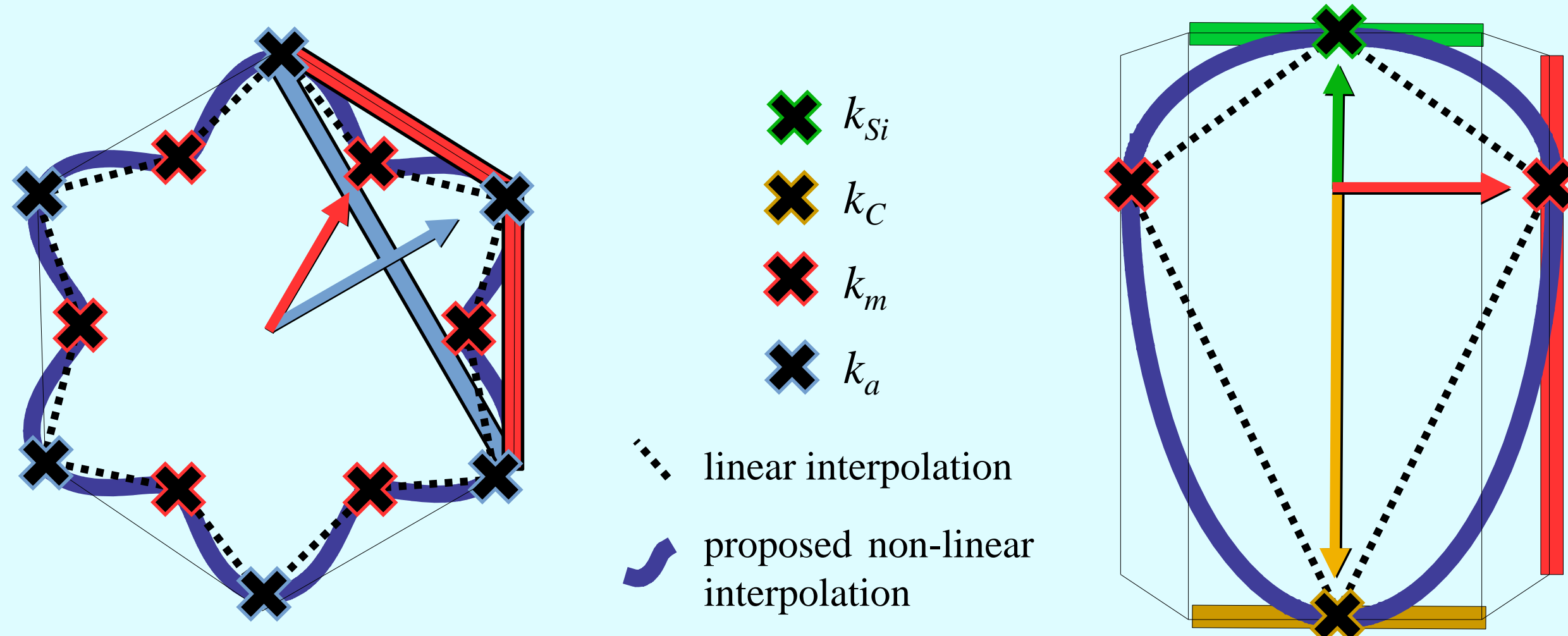
- $B/A \rightarrow$ linear rate constant
- $B \rightarrow$ parabolic rate constant
- $C \rightarrow$ exponential prefactor
- $L \rightarrow$ characteristic length
- All parameters depend highly on the crystal orientation of SiC.
- Due to the one-dimensional nature those models cannot correctly predict oxidation growth for three-dimensional SiC structures.
- We extend these models by incorporating the crystal direction dependence into the oxidation growth rates.

Interpolation Method

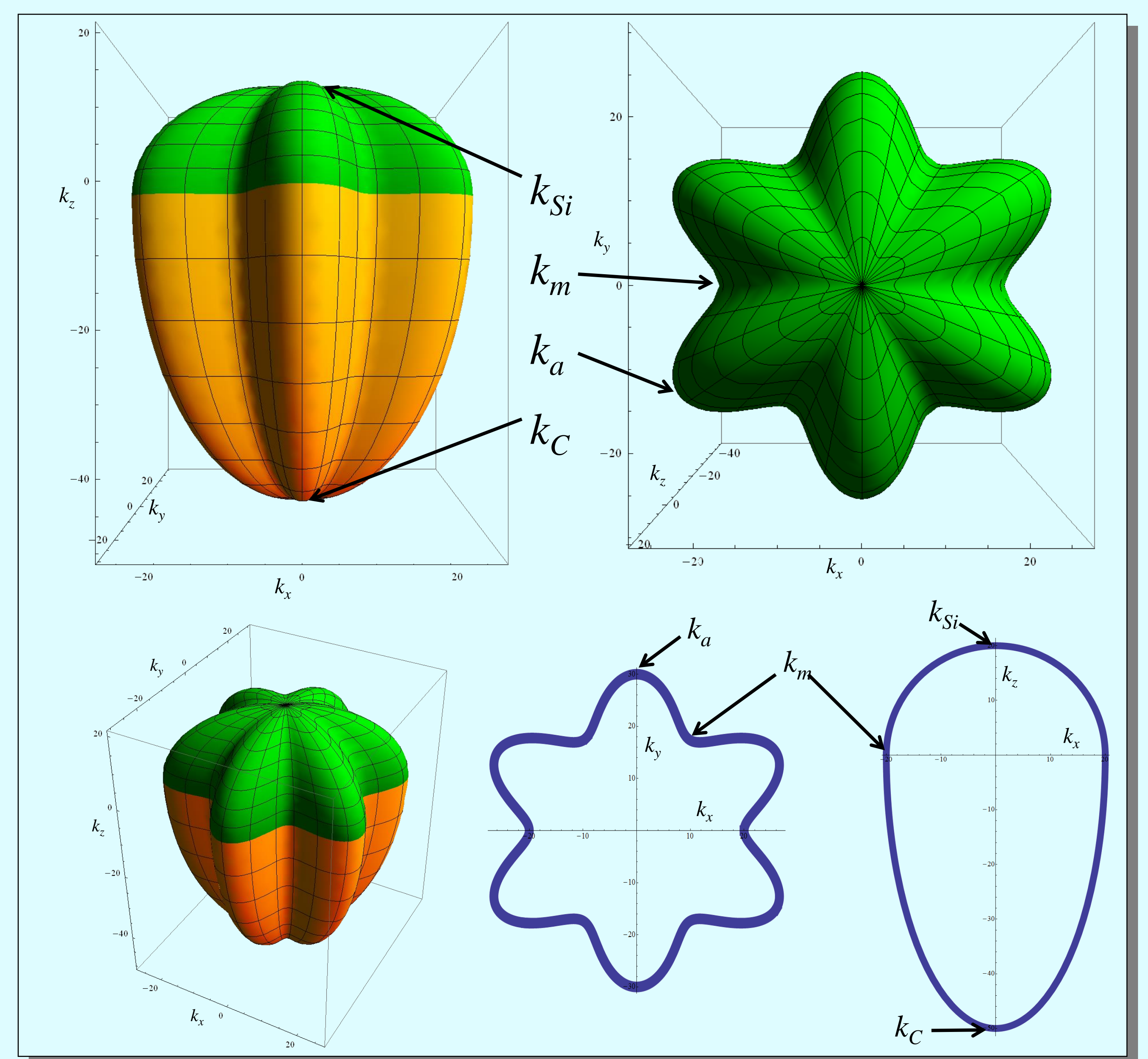
- The non-linear interpolation is written as a parametric function.
- A symmetric star shape in the x - y plane and a tangent-continuous union of two half-ellipses in z direction are used:

$$\begin{aligned} x &= \left(k_y + (k_x - k_y) \cos^2(3t)\right) \cos(t) \cos(u) \\ y &= \left(k_y + (k_x - k_y) \cos^2(3t)\right) \sin(t) \cos(u) \\ z &= k_z^+ \sin(u) \text{ for } u \geq 0 \\ z &= k_z^- \sin(u) \text{ for } u < 0 \end{aligned}$$

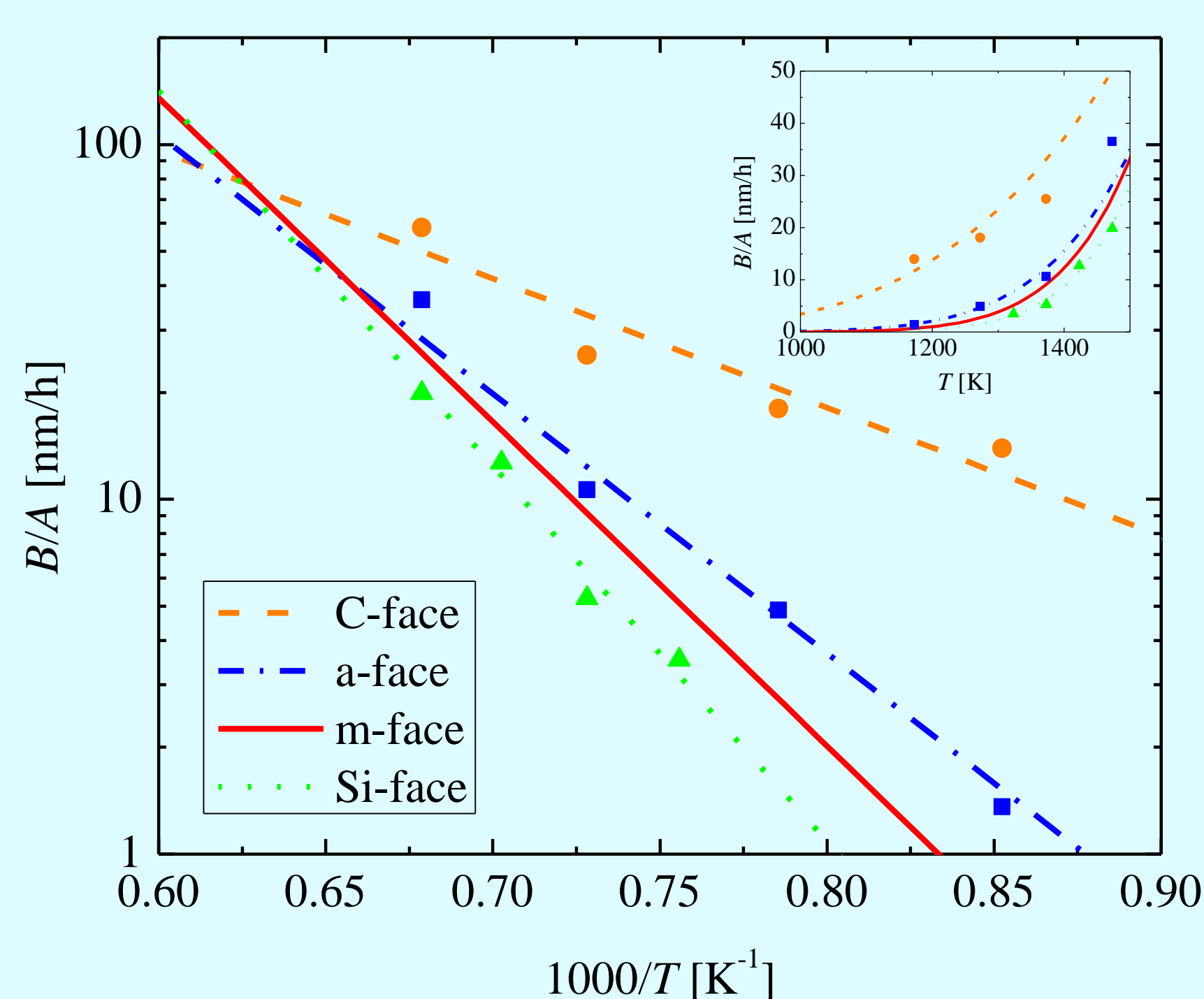
- $t \in [0, 2\pi]$ and $u \in [-\pi/2, \pi/2] \rightarrow$ arbitrary parametric variables
- $k_{x,y,z} \rightarrow$ known oxidation growth rates in x , y , and z direction



Results – The Growth Rate Surface



Growth Rates – Arrhenius Plot



- The relation between the temperature and the rate constant of the chemical reaction is defined by an Arrhenius equation:

$$k = Z \exp\left(-\frac{E_a}{RT}\right)$$

- We have obtained the growth rates and activation energies of the Si-, a-, and C-face from experimentally measured data [3].
- We have approximated the growth rate and activation energy for the m-face, based on published oxide thicknesses [4].

Conclusions

- The proposed interpolation method matches with the three-dimensional behavior of SiC oxidation.
- The method converts an arbitrary crystal direction into a growth rate value according to four known growth rate values.
- The necessary growth rates are provided with Arrhenius plots.

Acknowledgement

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