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A note on Segre varieties in characteristic two

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Let $\mathbf{V}_1, \mathbf{V}_2, \dots, \mathbf{V}_m$ be $m \geq 1$ two-dimensional vector spaces over the same commutative field F . The non-zero decomposable tensors of $\bigotimes_{k=1}^m \mathbf{V}_k$ determine the *Segre variety* $\mathcal{S}_{(m)}(F)$ in the projective space $\mathbb{P}(\bigotimes_{k=1}^m \mathbf{V}_k)$. Each \mathbf{V}_k admits a symplectic bilinear form $[\cdot, \cdot]$, so that $\bigotimes_{k=1}^m \mathbf{V}_k$ is equipped with a bilinear form which is given by

$$[\mathbf{a}_1 \otimes \mathbf{a}_2 \otimes \dots \otimes \mathbf{a}_m, \mathbf{b}_1 \otimes \mathbf{b}_2 \otimes \dots \otimes \mathbf{b}_m] := \prod_{k=1}^m [\mathbf{a}_k, \mathbf{b}_k] \quad \text{for } \mathbf{a}_k, \mathbf{b}_k \in \mathbf{V}_k.$$

In projective terms this form yields the well known *fundamental polarity* of $\mathcal{S}_{(m)}(F)$. It is associated to a regular quadric when m is even and $\text{Char } F \neq 2$. Otherwise it is a null polarity.

In our talk we focus on the case when F has characteristic two. Here the fundamental polarity of $\mathcal{S}_{(m)}(F)$ is always null, and there exists an *invariant quadric*:

Theorem. *Let $m \geq 2$ and $\text{Char } F = 2$. There exists in the ambient space of the Segre $\mathcal{S}_{(m)}(F)$ a regular quadric $\mathcal{Q}(F)$ with the following properties:*

1. *The projective index of $\mathcal{Q}(F)$ is $2^{m-1} - 1$.*
2. *$\mathcal{Q}(F)$ is invariant under the group of projective collineations stabilising the Segre $\mathcal{S}_{(m)}(F)$.*

This is joint work with Boris Odehnal (Vienna, Austria) and Metod Saniga (Tatranská Lomnica, Slovakia).

References

- [1] H. Havlicek, B. Odehnal, and M. Saniga. On invariant notions of Segre varieties in binary projective spaces. *Des. Codes Cryptogr.* 62 (2012), 343–356.