# Kinematics of a Human Steering a Car

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### Introduction

There are various approaches for steering a car, including different grips and angles at which the hand is in contact with the steering wheel. Two such grips are analyzed for their kinematic optimality by turning the steering wheel about +90deg, where the starting configuration is given in the drawings below. Therefore, different optimality measures and a model of the human arm are used.







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#### Manipulability

For steering the translation of the end-effector determines the rotation of the steering wheel. Thus only the position part is used in the Jacobian matrix, i.e.  $J \in \mathbb{R}^{3 \times 7}$ , on which the manipulability

$$m = \sqrt{\det(J(q)J^{\mathrm{T}}(q))}$$

is based. Turning the steering wheel is achieved by moving the hand tangent to the steering wheel. This movement can be described by joint movements mapped through the Jacobian matrix. Thus, the directional manipulability is proposed.

$$m_d = \max t^{\mathrm{T}} J \dot{q}$$

- Human arm modeled as 7R robot to analyze movements
- Optimization based inverse kinematics
- Kinematic motion analysis using manipulability measures
- Optimize seat position for manipulability

# 7R arm model



- Shoulder joint modeled with fixed position
- 7R model of the arm
- Forward kinematics using DH-convention







## Inverse Kinematics

In order to obtain the joint angles of the model corresponding to a prespecified steering maneuver an optimization was set up. An analytical solution to the inverse kinematics was not used, since the relative weighting of position and orientation allows for a realistic approximation of human behavior.

$$q = \arg \min_{q} \sum_{k=1}^{N} (f(q_{k}) - p_{k,ref})^{\mathrm{T}} (f(q_{k}) - p_{k,ref}) + (o_{v,k} - o_{v,k,ref})^{\mathrm{T}} W_{o}(o_{v,k} - o_{v,k,ref}) + (q_{k+1} - q_{k})^{\mathrm{T}} W_{\Delta q}(q_{k+1} - q_{k}) + q_{k}^{\mathrm{T}} W_{q} q_{k}$$

The terms of this formula (in order of appearance) corresponding to the

Position error

Orientation error

In order to calculate the optimal position of the driver seat the optimization problem is solved for different shoulder joint positions. The integrated manipulability is used as cost function to determine the optimal shoulder position.

$$M = \int_0^{90^\circ} m(\varphi) \mathrm{d}\varphi$$

**Optimal seat position** 

$$M_d = \int_0^{90^\circ} m_d(\varphi) \mathrm{d}\varphi$$



Note: The red dots in the figures above show the manipulability M and the directional manipulability  $M_d$  for the nominal shoulder position.

# Results



Directional manipulability suggest the shoulder to be far away from the steering wheel (Note that this conflicts with forcemanipulability)

Manipulability gives a distinct optimal distance to the steering wheel (different measures are possible)

Seat height has little influence on the manipulability

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