Types of self-motions of planar Stewart Gough platforms

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With this talk, which is based on reference [1], we want to continue the series of contributions about selfmotions of Stewart Gough platforms given by KARGER [2, 3] in the previous conferences on geometry – theory and applications, held in Vorau 2007 and Plzen 2009.

We show that the self-motions of the general planar Stewart Gough platforms can be characterized in the complex extension of the Euclidean 3-space by the movement of three platform points in planes orthogonal to the planar base (3-point Darboux motion; cf. [4]) and a simultaneous sliding of three planes orthogonal to the planar platform through points of the base (3-plane Mannheim motion; cf. [4]). Based on this consideration, we can prove that all one-parametric self-motions of a general planar Stewart Gough platform can be classified into two types (type I DM and type II DM, where DM abbreviates Darboux Mannheim).

We also present a way on how the set of equations yielding a type II DM self-motion can be computed explicitly. Based on these equations, which are of great simplicity seen in the context of self-motions, we are also able to compute first results for this class of self-motions (cf. [5]). These results raise the hope of giving a complete classification of type II DM self-motions in the future, which would be an important step in solving the famous Borel Bricard problem [3, 6, 7, 8, 9]. The work towards this goal is in progress.

We close the talk by presenting a geometric interpretation of a large set of already known type II DM self-motions (cf. [2, 10]), which also simplifies their computation considerably.

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